

# Determination of Electroweak Parameters

Seminar 'Particle Physics at the LHC'

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# Introduction



- ▶ el.weak interaction: unification of electromagnetism ( $\gamma$ ) and weak interaction (Fermi / V-A theory /  $W^\pm$ )
- ▶ structure:  $SU(2)_L \times U(1)_Y$  (fields:  $W_1, W_2, W_3, B$ )
- ▶ predicts additional particle ( $Z^0$ )  $\rightarrow$  first evidence in bubble chamber at CERN ( $\bar{\nu}_\mu e^-$  scattering, 1973)
- ▶ discovery of Higgs boson ( $\rightarrow m_H$ ) allows for consistency check.

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- ▶ experimental fact:  $m_Z$  well known (LEP),  
 $m_Z = 91\,188 \pm 2$  MeV [3]
- ▶ relations in el. weak theory (Born level):

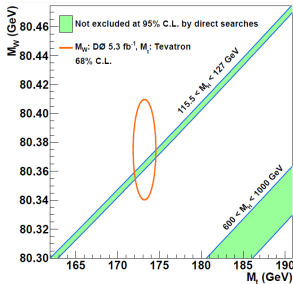
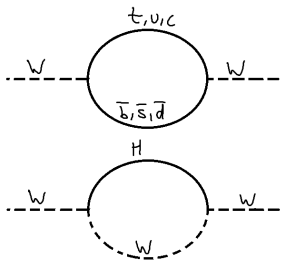
$$e = g \sin \theta_W = g' \cos \theta_W, \quad m_W = m_Z \cos \theta_W,$$
$$G_F = \frac{\sqrt{2}g^2}{8m_W^2}, \quad \alpha = \frac{e^2}{4\pi}, \quad m_H = v\sqrt{2\lambda} = \frac{\sqrt{8\lambda}m_W}{g}$$

⇒ 4 independent parameters

# Introduction



- ▶ additional relations by higher orders:



→ contributions to  $m_W$ :  $\sim (m_u - m_d)^2$  and  $\sim \log m_H/m_W$  respectively.

- ▶ significant contribution from  $m_t$
- ▶ additional contributions from new particles (SUSY)

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# Template Method



create simulations (distributions) for multiple values of physics parameter  $m$  in observable  $d$  ( $p_T, m_T, E_T^{\text{miss}}, \dots$ )



interpolate between samples with continuous function (fitting, determine arbitrary parameters  $p_j$ ), axis:  $m, d$

$$f(m, d, p_j)$$



fit function to data with fixed  $p_j$ , determine  $m$

$$f(m, d, p_j)$$

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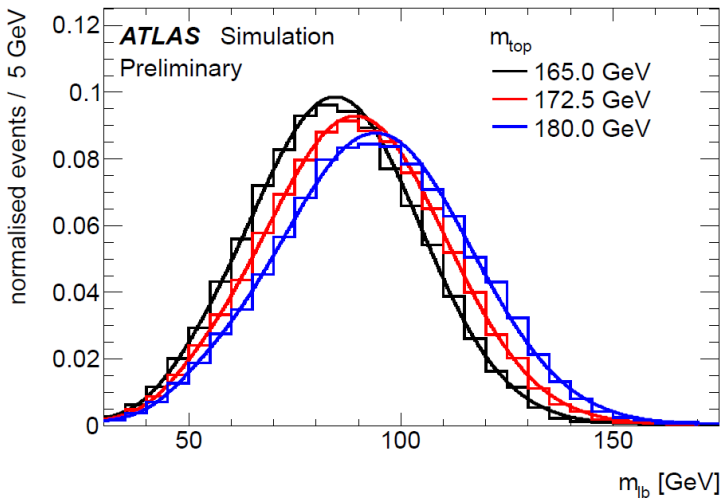
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# Template Method



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# Mass of the W Boson



- ▶ main production channel:  $q\bar{q}' \rightarrow W + X$  (X=hadr. recoil, gluon ISR)
- ▶ decay channel for measurement:  $W \rightarrow \ell\nu$ ,  $\ell = e, \mu$  (low background, BR  $\approx 22\%$ )
- ▶  $m_W$  measurement via kinematic distributions
- ▶ so far: only Tevatron results ( $\sqrt{s} = 1.96$  TeV,  $\sim 2 - 5$  fb $^{-1}$ ,  $p\bar{p}$ )

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# Mass of the W Boson - Variables



frequently used variables:

- ▶ transverse momentum  $p_T^\ell = p^\ell \cdot \cos \theta$
- ▶ transverse mass (for  $W \rightarrow e\nu$ ):

$$m_T = \sqrt{2p_T^e p_T^\nu (1 - \cos \Delta\phi)}$$

- ▶ missing transverse momentum / energy:

$$p_T^{\text{miss}} = E_T^{\text{miss}} = \left| \sum_{i \in \text{event}} \vec{p}_T^i \right| = p_T^\nu$$

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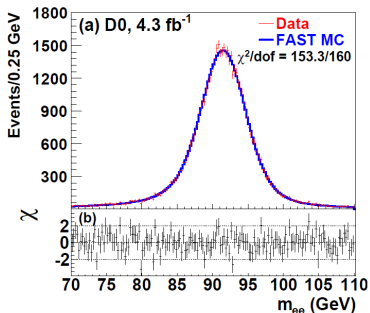
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# Mass of the W Boson @ D0 (2012)



- ▶ Z boson mass for calibration of el.mag.-calorimeter and hard.-calorimeter, only  $W \rightarrow e\nu$  for measurement
- ▶ el.mag.-calorimeter:  $E^{\text{meas}} = \alpha E^{\text{true}} + \beta \rightarrow$  fit of  $m_{ee}$ ,  $E_e$ ,  $\phi_{ee}$  for  $Z \rightarrow ee$  events
- ▶ hadr.-cal.: use projection of  $\vec{p}_T^{ee} + \vec{u}_T$  ( $u_T =$  E-deposits w/o  $p_T^{ee}$ ) onto axis  $\vec{e}^{\ell_1} + \vec{e}^{\ell_2}$



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# Mass of the W Boson @ D0 (2012)



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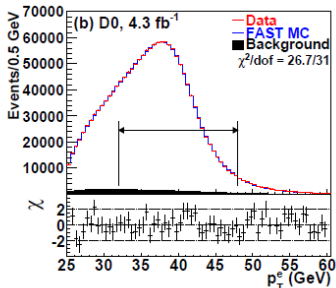
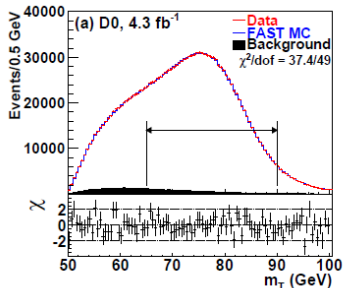
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- ▶ event requirements: high  $p_T^e, E_T^{\text{miss}} > 25$  GeV, small (hadronic) recoil ( $< 15$  GeV),  $m_T \in (50, 200)$  GeV
- ▶ template method with  $d = m_T, p_T^e, E_T^{\text{miss}}$



- ▶ combined result:  $m_W = 80.367 \pm 0.013 \pm 0.022$  GeV [1]

# Mass of the W Bosons @ D0 (2012)



TABLE II: Systematic uncertainties of the  $M_W$  measurement.

Source	$\Delta M_W$ (MeV)		
	$m_T$	$p_T^e$	$E_T$
Electron energy calibration	16	17	16
Electron resolution model	2	2	3
Electron shower modeling	4	6	7
Electron energy loss model	4	4	4
Hadronic recoil model	5	6	14
Electron efficiencies	1	3	5
Backgrounds	2	2	2
Experimental subtotal	18	20	24
PDF	11	11	14
QED	7	7	9
Boson $p_T$	2	5	2
Production subtotal	13	14	17
Total	22	24	29

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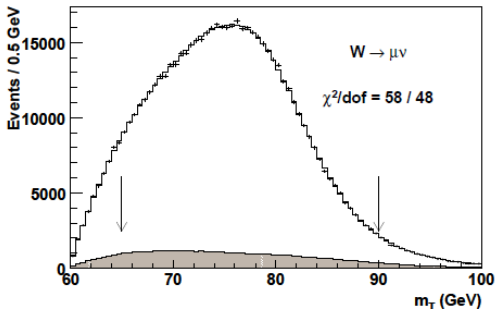
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# Mass of the W Boson @ CDF (2013)



- ▶ momentum scale calibration:  $J/\psi, \Upsilon \rightarrow \mu\mu$ , compare simulation + data
- ▶ energy scale: use  $E/p$  peak in  $Z \rightarrow ee$  ( $S_E$  extracted through likelihood fit)
- ▶  $W \rightarrow e\nu$  and  $W \rightarrow \mu\nu$  used, same kinematic variables as D0



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# Mass of the W Boson @ CDF (2013)



Source	$m_T$ fit uncertainties		
	$W \rightarrow \mu\nu$	$W \rightarrow e\nu$	Common
Lepton energy scale	7	10	5
Lepton energy resolution	1	4	0
Lepton efficiency	0	0	0
Lepton tower removal	2	3	2
Recoil scale	5	5	5
Recoil resolution	7	7	7
Backgrounds	3	4	0
PDFs	10	10	10
$W$ boson $p_T$	3	3	3
Photon radiation	4	4	4
Statistical	16	19	0
Total	23	26	15

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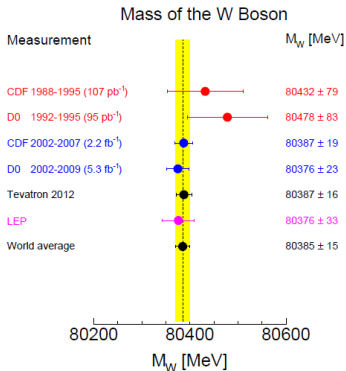
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result:  $m_W = 80.387 \pm 0.012 \pm 0.015$  GeV [2] ( $2.2 \text{ fb}^{-1}$ )

# Mass of the W Boson @ Tevatron (2013)



- ▶ combination → account for correlations (collider, simulation software, calibration method,...)



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# Mass of the top Quark

- ▶ decay mainly via  $t \rightarrow bW$
- ▶ analysis channels ( $t\bar{t}$ ): di lep ( $WW \rightarrow \ell\nu\ell'\nu'$ , BR = 4%), lep+jets ( $WW \rightarrow \ell\nu q\bar{q}'$ , BR = 29%), all jets (BR = 45 %)
- ▶ event selection via *b-tagging*, ATLAS: neural-net using topology of  $t$  decay (efficiency:  $\sim 70\%$  of  $b$ -jets,  $\sim 1/130$  light quark jets)

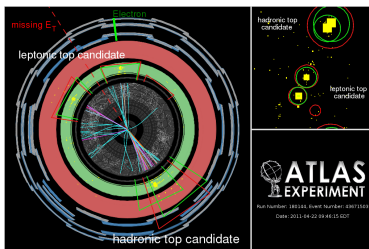
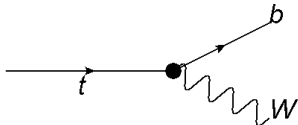
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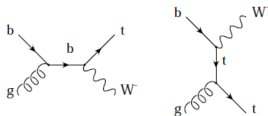




# Mass of the top Quark (Dileptonic, ATLAS)



- ▶  $\sqrt{s} = 7 \text{ TeV}$ ,  $4.7 \text{ fb}^{-1}$
- ▶ requirements: = 2 b-tagged jets, high  $E_T^{\text{miss}}$ , = 2 opposite charge leptons,  $\geq 2$  central jets with  $p_T > 25 \text{ GeV}$
- ▶ main backgrounds: single  $t$  via  $Wt$  production,  $Z \rightarrow \ell^+ \ell^-$



- ▶ strict selection  $\rightarrow$  background is small
- ▶ method: template method

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# Mass of the top Quark (Dileptonic, ATLAS)



kinematic variable  $m_{\ell b}$ :

- ▶ two possible combinations of  $\ell + b$  per event
- ▶ two invariant masses per combination  $\rightarrow$  calculate average
- ▶  $m_{\ell b}$  is the lower avg. inv. mass

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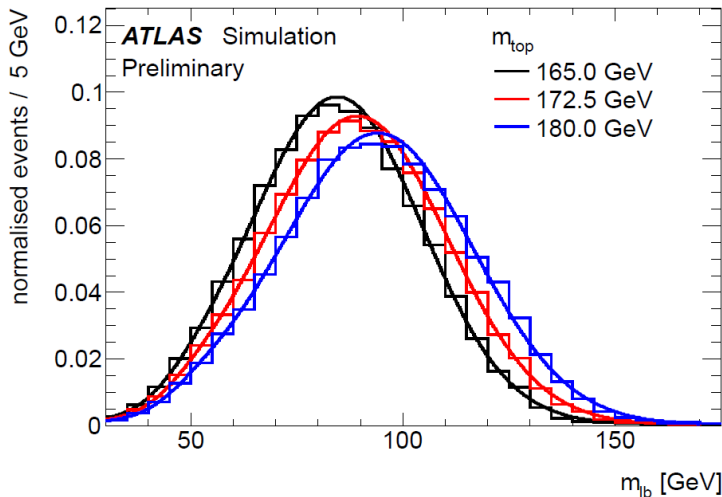
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# Mass of the top Quark (Dileptonic, ATLAS)



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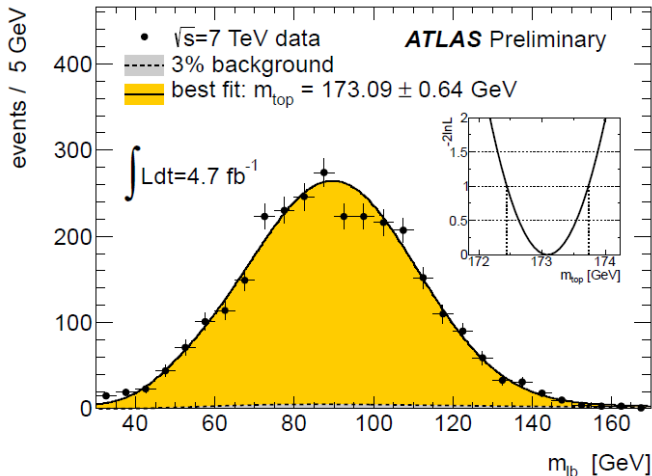
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# Mass of the top Quark (Dileptonic, ATLAS)



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# Mass of the top Quark (Dileptonic, ATLAS)



Description	Value [GeV]
Measured value	173.09
Statistical uncertainty	0.64
Method calibration	0.07
Signal MC generator	0.20
Hadronisation	0.44
Underlying event	0.42
Colour reconnection	0.29
ISR/FSR	0.37
Proton PDF	0.12
Background	0.14
Jet energy scale	0.89
<i>b</i> -jet energy scale	0.71
<i>b</i> -tagging efficiency and mistag rate	0.46
Jet energy resolution	0.21
Missing transverse momentum	0.05
Pile-up	0.01
Electron uncertainties	0.11
Muon uncertainties	0.05
Total systematic uncertainty	1.50
Total uncertainty	1.63

Table 2: The measured value of  $m_{\text{top}}$  and the contributions of the various sources detailed in the text to the total systematic uncertainty.

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# Mass of the top Quark (lep+jets, ATLAS)



- ▶  $\sqrt{s} = 7 \text{ TeV}$ ,  $1.04 \text{ fb}^{-1}$
- ▶ requirements: 2 b-jets,  $\geq 4$  central jets with  $p_T > 25 \text{ GeV}$ , = 1 lepton,  $E_T^{\text{miss}} > 20 \text{ GeV}$
- ▶ most precise channel, advantages compared to
  - dilep full reconstruction (only 1  $\nu$ )
  - all jets easier matching
- ▶ two subanalyses

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# Mass of the top Quark (lep+jets, ATLAS): 1d



1d-analysis:

- ▶ variable (for  $t \rightarrow bW$ ,  $W \rightarrow \text{had}$ ):

$$R_{32} \equiv \frac{m_{\text{top}}^{\text{reco}}}{m_W^{\text{reco}}}$$

- cancellation of uncertainties
- ▶ selection of jets via kinematic likelihood fit

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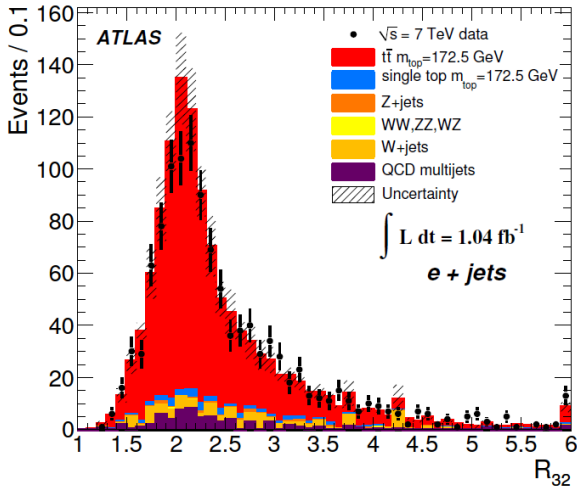
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# Mass of the top Quark (lep+jets, ATLAS): 1d



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# Mass of the top Quark (lep+jets, ATLAS): 2d



## 2d-analysis:

- ▶ fitting probability density functions in  $(m_{\text{top}}^{\text{reco}}, m_W^{\text{reco}})$  plane to data
- ▶ use known  $m_W$  and  $\Gamma_W$  for  $m_{\text{top}}^{\text{reco}}$  reconstruction
- ▶ free fit parameters:  $m_t, JSF, n_{\text{bkg}}$  → "in situ jet scaling"  
⇒ shifting syst. → stat. uncertainty

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# Mass of the top Quark (lep+jets, ATLAS)



results:

$$m_{t,1d} = 174.4 \pm 0.9 \pm 2.5 \text{ GeV}, m_{t,2d} = 174.5 \pm 0.6 \pm 2.3 \text{ GeV} [5]$$

	1d-analysis		2d-analysis		Combinations		Correlation $\rho$
	$e+\text{jets}$	$\mu+\text{jets}$	$e+\text{jets}$	$\mu+\text{jets}$	1d	2d	
Measured value of $m_{\text{top}}$	172.93	175.54	174.30	175.01	174.35	174.53	
Data statistics	1.46	1.13	0.83	0.74	0.91	0.61	
Jet energy scale factor	na	na	0.59	0.51	na	0.43	0
Method calibration	0.07	< 0.05	0.10	< 0.05	< 0.05	0.07	0
Signal MC generator	0.81	0.69	0.39	0.22	0.74	0.33	1
Hadronisation	0.33	0.52	0.20	0.06	0.43	0.15	1
Pileup	< 0.05	< 0.05	< 0.05	< 0.05	< 0.05	< 0.05	1
Underlying event	0.06	0.10	0.42	0.96	0.08	0.59	1
Colour reconnection	0.47	0.74	0.32	1.04	0.62	0.55	1
ISR and FSR (signal only)	1.45	1.40	1.04	0.95	1.42	1.01	1
Proton PDF	0.22	0.09	0.10	0.10	0.15	0.10	1
$W+\text{jets}$ background normalisation	0.16	0.19	0.34	0.44	0.18	0.37	1
$W+\text{jets}$ background shape	0.11	0.18	0.07	0.22	0.15	0.12	1
QCD multijet background normalisation	0.07	< 0.05	0.25	0.33	< 0.05	0.20	(1)
QCD multijet background shape	0.14	0.12	0.38	0.30	0.09	0.27	(1)
Jet energy scale	1.21	1.25	0.63	0.71	1.23	0.66	1
$b$ -jet energy scale	1.09	1.21	1.61	1.53	1.16	1.58	1
$b$ -tagging efficiency and mistag rate	0.21	0.13	0.31	0.26	0.17	0.29	1
Jet energy resolution	0.34	0.38	0.07	0.07	0.36	0.07	1
Jet reconstruction efficiency	0.08	0.11	< 0.05	< 0.05	0.10	< 0.05	1
Missing transverse momentum	< 0.05	< 0.05	0.12	0.16	< 0.05	0.13	1
Total systematic uncertainty	2.46	2.56	2.31	2.57	2.50	2.31	
Total uncertainty	2.86	2.80	2.46	2.68	2.66	2.39	

stat. correlation 1d  $\leftrightarrow$  2d : < 50% (different jet triplet selection +  $m_{\text{top}}$  estimator)

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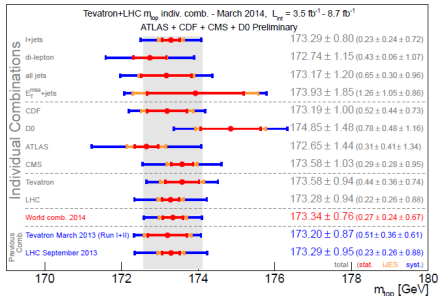
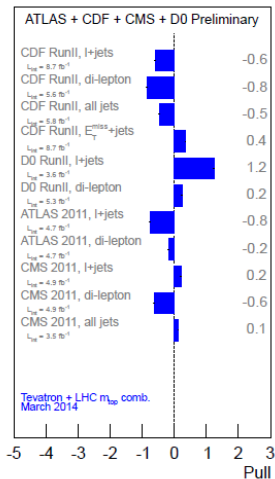
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# Mass of the top Quark (Combination)



consistent results:



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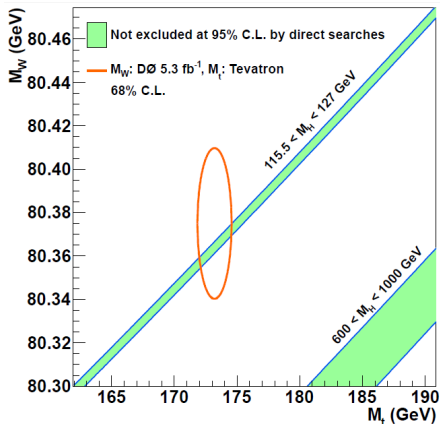
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# Test of the Standard Model



- ▶  $m_W$  and  $m_t$  give constraints on  $m_H$  before summer 2012:



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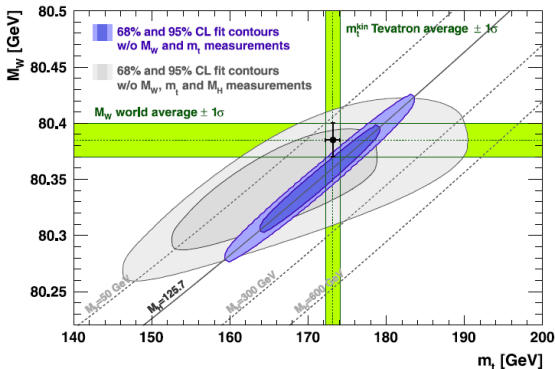
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# Test of the Standard Model



and after:



shifted focus: prediction of  $m_H \rightarrow$  testing consistency of SM  $\rightarrow \sigma_{m_W}$  is limiting!

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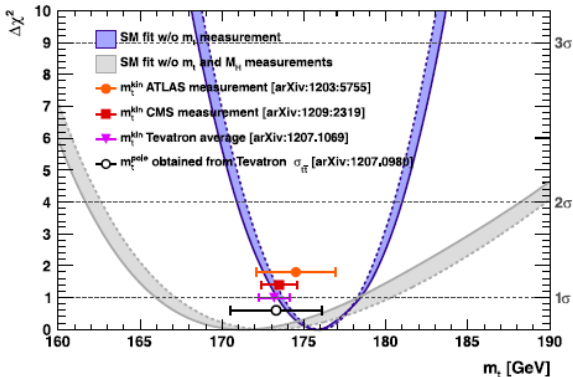
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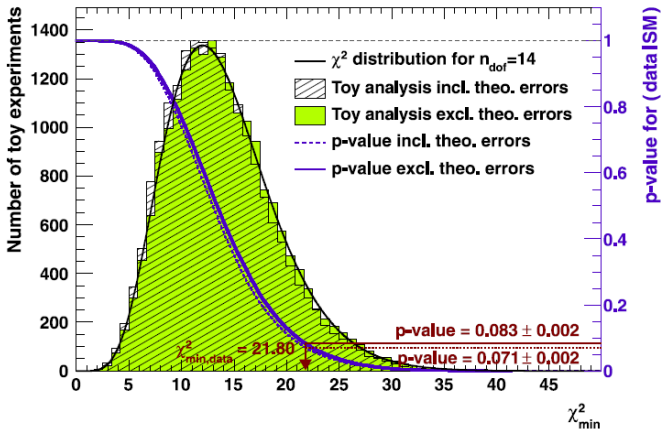
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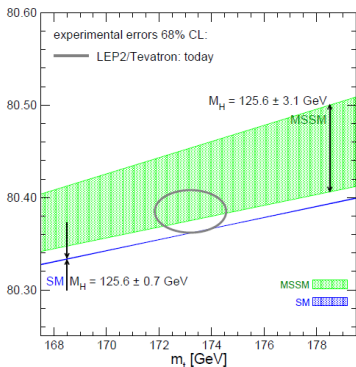


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# Test of the Standard Model - new physics?



for light ( $m_H = 125.6$  GeV) CP even Higgs boson (MSSM: 5 Higgs bosons)



→  $\sigma_{m_w}$  is limiting!

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# Summary



- ▶ W-mass:  $80385 \pm 15$  MeV (syst. limited!)
- ▶ top-mass:  $173340 \pm 760$  MeV (syst. limited!)
- ▶ standard model compatible with measurements ( $p \approx 8\%$ )
- ▶ exclusions/hints on new physics limited by  $m_W$  precision

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The End



Thanks for your attention!

Questions? Remarks?

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# top-Mass ( $\Delta m_{t,\bar{t}}$ )

- ▶ CPT invariance requires  $\Delta m = m_t - m_{\bar{t}} = 0$
- ▶ ATLAS:  $\sqrt{s} = 7 \text{ TeV}$ ,  $4.7 \text{ fb}^{-1}$ , template method, variable

$$\Delta_m^{\text{fit}} = q\ell \cdot \left( m_{b\ell\nu}^{\text{fit}} - m_{bjj}^{\text{fit}} \right)$$

→ cancellation of systematic uncertainties. Result:  
 $\Delta m = 0.67 \pm 0.61 \pm 0.41$  [8]

- ▶ other results (from [8]):
  - ▶ CDF:  $\Delta m = 3.3 \pm 1.4 \pm 1.0 \text{ GeV}$
  - ▶ D0 :  $\Delta m = 0.8 \pm 1.8 \pm 0.5 \text{ GeV}$
  - ▶ CMS:  $\Delta m = -0.44 \pm 0.46 \pm 0.27 \text{ GeV}$
- ▶ ⇒ compatible with  $\Delta m = 0$

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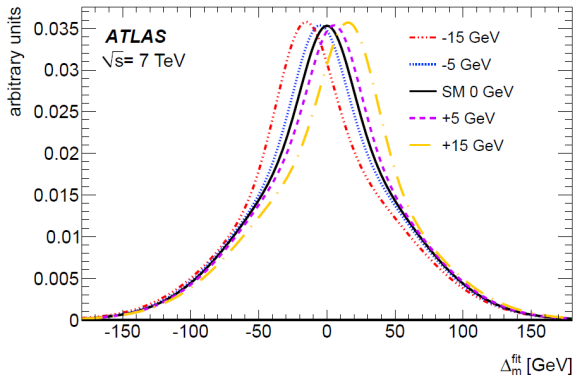
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# top-Mass ( $\Delta m_{t,\bar{t}}$ )



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